Parameter-Free Centralized Multi-Task Learning for Characterizing Developmental Sex Differences in Resting State Functional Connectivity

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Abstract
In contrast to most existing studies that typically characterize the developmental sex differences using analysis of variance or equivalently multiple linear regression, we present a parameter-free centralized multi-task learning method to identify sex specific and common resting state functional connectivity (RSFC) patterns underlying the brain development based on resting state functional MRI (rs-fMRI) data. Specifically, we design a novel multi-task learning model to characterize sex specific and common RSFC patterns in an age prediction framework by regarding the age prediction for males and females as separate tasks. Moreover, the importance of each task and the balance of these two patterns, respectively, are automatically learned in order to make the multi-task learning robust as well as free of tunable parameters, i.e., parameter-free for short. Our experimental results on synthetic datasets verified the effectiveness of our method with respect to prediction performance, and experimental results on rs-fMRI scans of 1041 subjects (651 males) of the Philadelphia Neurodevelopmental Cohort (PNC) showed that our method could improve the age prediction on average by 5.82% with statistical significance than the best alternative parameters, i.e., parameter-free for short. Our experimental results on synthetic datasets verified the effectiveness of our method with respect to prediction performance, and experimental results on rs-fMRI scans of 1041 subjects (651 males) of the Philadelphia Neurodevelopmental Cohort (PNC) showed that our method could improve the age prediction on average by 5.82% with statistical significance than the best alternative methods under comparison, in addition to characterizing the developmental sex differences in RSFC patterns.

Introduction
Adolescence is the developmental period during which functional brain maturation interacts with sexual divergence in social, behavior, and biological changes (Kochhann et al. 2017). Particularly, sex differences are prominent in behavior and have been studying for a long time (Hardee et al. 2017; Qian et al. 2015a). For instance, females are superior at social cognition and recognition memory than males, while males perform better in visuospatial and motor tasks than females (Gur and Gur 2016).

It is of great importance to understand the neural origins of the developmental sex differences in behavior as both sex differences and brain structure/function are shaped during adolescence to support the brain development and neuropsychiatric disorders typically begin in adolescence and are linked to aberrations in neurodevelopment (Di Martino et al. 2014). Recently, neuroimaging measures, including both structural and functional neuroimaging measures, have been adopted as surrogate neural variables for exploring neural origins of the developmental sex differences (Ingahalikar et al. 2014; Alarcón et al. 2015). Particularly, magnetic resonance imaging (MRI) is a widely used technique for sex differences analysis (Gur and Gur 2016). Several studies on sex differences via analyzing gray matter (GM) and white matter (WM) of the brain MRI data have reported that females have smaller brain volume and cerebral spinal fluid (CSF) volume than males, and CSF volume changes faster in males than in females (Blakemore, Burnett, and Dahl 2010).

Resting state functional MRI (rs-fMRI) provides task-independent and relatively reproducible biomarkers of functional coherence of activity in different brain regions (Fox and Raichle 2007). Using resting state functional connectivity (RSFC) analytic techniques, we are able to investigate the brain functional organization of both typical brain development and neuropsychiatric disorders (Fox and Raichle 2007; Di Martino et al. 2014) and we can also characterize the brain state at an individual subject level based on the RSFC measures using pattern recognition techniques (Fan and Davatzikos 2017). Recent studies have demonstrated that RSFC measures are more accurate than cognitive profiles for both sex classification and sex differences characterization, and males exhibit weaker nucleus accumbens functional connectivity than females in adolescent brains (Müller-Oehring et al. 2017).

Since brain development differs between males and females across adolescence (Ingahalikar et al. 2014; Alarcón et al. 2015), the interaction of age and sex on RSFC has been investigated using analysis of variance (ANOVA) or equivalently multiple linear regression for exploring neural origins of sex differences in the developing brain (Alarcón et al. 2015). However, such analytic tools are typically adopted in a univariate statistical analysis, not equipped to characterize multivariable relationships, such as the interaction of age and sex on the functional brain network which is typically characterized by a set of edgewise RSFC measures (Alarcón et al. 2015).

In order to robustly characterize the interaction of sex and age on the RSFC measures in a multivariate analy-
sis setting, we present a parameter-free centralized multi-task learning method to identify sex specific and common RSFC patterns underlying the brain development based on rs-fMRI data in an age prediction framework. Specifically, our method explicitly identifies two sets of RSFC measures, namely male specific and female specific RSFC measures, which contribute differently to the age prediction by modeling the age prediction for males and females as separate tasks in a multi-task learning framework. At the same time, the male specific and female specific RSFC measures are regularized to be sparse and centralized to have a shared, sex common pattern by optimizing a square root objective function that models difference between measured and predicted ages with an $\ell_2,1$-norm regularization (Hu et al. 2017; Zhu et al. 2017b; 2016b; Peng and Fan 2016). The importance of each task and the balance of these two patterns, respectively, are automatically learned to make the multi-task learning free of tunable parameters, i.e., parameter-free for short. As a result, the parameter-free, centralized, sparse multi-task learning makes our method fast and robust to noisy measures/outhiers. Akin to the ANOVA method, the sex specific RSFC patterns characterize sex differences while the sex common RSFC patterns characterize the interaction effect of sex and age on the developing RSFC measures. Furthermore, our method may make these two patterns collaboratively help each other to improve the prediction performance of each task and discover more interesting patterns which cannot be found in a model built on data from only one sex group.

We have validated our method based on synthetic and real datasets. Our experimental results on synthetic datasets verified the effectiveness of our method with respect to the age prediction performance. We also investigated the development sex differences in RSFC measures based on rs-fMRI data of 1041 subjects (651 males) of the Philadelphia Neurodevelopmental Cohort (PNC) dataset (Li, Satterthwaite, and Fan 2017). Our experimental results showed that our method could improve the age prediction on average by 5.82% with statistical significance than the best alternative methods under comparison, including state-of-the-art multi-task learning methods, sex specific age prediction models, and an age prediction model with sex as a feature, in addition to characterizing the developmental sex differences in RSFC patterns.

**Methods**

In this paper, we denote matrices as boldface uppercase letters, vectors as boldface lowercase letters, and scalars as normal italic letters. For a matrix $X = [x_{ij}]$, its $i$-th row and $j$-th column are denoted as $x^i$ and $x_j$, respectively. We also denote the Frobenius norm and the $\ell_1$-norm of a matrix $X$ as $\|X\|_F = \sqrt{\sum_j \|x_j\|_2^2}$ and $\|X\|_1 = \sum_{ij} |x_{ij}|$, respectively. We denote the transpose operator, the trace operator, and the inverse of a matrix $X$ as $X^T$, $tr(X)$, and $X^{-1}$, respectively.

**Sparse feature selection**

Given an RSFC feature matrix $X \in \mathbb{R}^{n \times d}$ and its associated age vector $y \in \mathbb{R}^n$, where $n$ and $d$, respectively, are the number of subjects and the dimensionality of RSFC features, we assume that there is a linear relationship between the RSFC features $X$ and the age vector $y$. We then use the least square loss function to measure their similarity or relationship via following formulation:

$$\min_w \|y - Xw\|_2^2,$$

(1)

where the coefficient vector $w \in \mathbb{R}^d$ maps $X$ to $y$ for achieving the minimal prediction residual $\|y - Xw\|_2^2$ and $Xw$ is the prediction of $y$.

The least square regression in Eq. (1) has a closed form solution, i.e., $(X^TX)^{-1}X^Ty$. However, the inverse operator is often ill-posed when dealing with high-dimensional data (Zhu et al. 2017a; Peng and Fan 2017a), e.g., the large number of $d$ ($d > n$) in the present study. In this case, a regularization is always recommended (Peng and Fan 2017b; Qian et al. 2015b; Chang et al. 2014; Zhu et al. 2017c). On the other hand, not all the features (i.e., functional connectivity measures between different nodes of the brain) are predictive for the brain development, i.e., the age prediction. To address above issues, we employ a sparse regularization to solve the ill-posed issue and select important features. We thus have following formulation:

$$\min_w \|y - Xw\|_2^2 + \lambda \|w\|_1,$$

(2)

where $\lambda \geq 0$ is a nonnegative tuning parameter, and a large value of $\lambda$ encourages sparsity of the model.

After solving Eq. (2), the features with zero coefficients in $w$ are regarded as unimportant features while the remaining features with nonzero coefficients are regarded as important features (Yang et al. 2015; Zhang et al. 2017). In this way, we may use Eq. (2) to conduct feature selection in the individual groups (i.e., the female group and the male group, respectively). We can also concatenate the data points in different groups to form a large dataset to build an age prediction model for each group.

**Parameter-free centralized multi-task learning**

According to existing studies of the developmental sex difference in RSFC patterns (Alarcón et al. 2015) and our experimental results summarized in Table 4, we observe that males and females develop differently with respect to their RSFC patterns, but share common developmental patterns. Therefore, we propose to simultaneously identify sex specific RSFC patterns and sex common patterns in a uniformed framework, with the expectation that these sex groups collaboratively help each other to improve the prediction performance and discover more interesting patterns, which cannot be found in a model built with only one sex group.

To do this, we regard the prediction of each group (i.e., the female group and the male group, respectively) as one task. We then denote the RSFC feature matrices as $X_1 \in \mathbb{R}^{n_1 \times d}$ and $X_2 \in \mathbb{R}^{n_2 \times d}$ (where $n_1$ and $n_2$, respectively, are the number of the subjects of these two tasks), and their corresponding age vectors as $y_1 \in \mathbb{R}^{n_1}$ and $y_2 \in \mathbb{R}^{n_2}$, respectively. It is noteworthy that our method can deal with cases where both the number of the subjects and the dimensions of the features are different in these two tasks. We further use
where the derivatives of the square root in Eq. (4) and obtain the
converges.

In this study, to achieve the goal that two different tasks collaboratively help each other, we use a centralized regulariza-
tion to penalize the variance of the coefficient vectors (i.e., \( w_t \), \( t = 1, \ldots, k \)) by optimizing following objective
function:

\[
\min_{w_t} \sum_{t=1}^{k} \| y_t - X_t w_t \|_2^2 + \gamma\| W \|_1, \tag{3}
\]

where \( W = [w_1, \ldots, w_k] \in \mathbb{R}^{d \times k} \) and \( \gamma \) is a nonnegative
tuning parameter to control the sparsity ratio of \( W \).

To solve the optimization problem of Eq. (4), i.e., optimiz-
ing the variables \( w_t \) (\( t = 1, \ldots, k \)) and \( \bar{w} \), we compute the
derivatives of the square root in Eq. (4) and obtain the follow-
ing formulation:

\[
\min_{w_t, \bar{w}} \sum_{t=1}^{k} \sqrt{\| y_t - X_t w_t \|_2^2 + \| w_t - \bar{w} \|_{2,1}} + \gamma\| W \|_1, \tag{4}
\]

We arrange Eq. (6a) to obtain the following formulation:

\[
\min_{w_t, \bar{w}} \sum_{t=1}^{k} \| y_t - \bar{X}_t w_t \|_2^2 + \gamma\| W \|_1 \tag{7}
\]

where \( \bar{X}_t = [\sqrt{\alpha_t X_t^T}, \sqrt{\beta_t \bar{X}_k} \bar{W}]^T \in \mathbb{R}^{(n+d) \times 1}, \bar{X}_k =
[\sqrt{\alpha_k X_k^T}, \sqrt{\beta_k \bar{X}_k} \bar{W}]^T \in \mathbb{R}^{(n+d) \times d}, \) and \( I \in \mathbb{R}^{d \times d} \) is an
identity matrix. Eq. (7) is a standard objective function of
sparse multi-task learning, which can be solved by the tool-
box MALSAR (Zhou, Chen, and Ye 2011).

The optimization of our objective function Eq. (4) may
obtain a local optimal solution. However, both the predic-
tion and the convergence of our method were insensitive
to the initialization because our method achieved good pre-
diction performance and fast convergence by only initializ-
ing \( w_t \) with the least square results, i.e., \( (X_t^T X_t + 0.001 * I)^{-1} X_t^T y_t \), and setting \( \bar{w} \)
the average of all \( w_t, \alpha_t = \frac{1}{k}, \) and \( \beta_t = \frac{1}{t}, \) \( t = 1, \ldots, k. \)

Our objective function in Eq. (4) brings several advan-
tages. Firstly, once Eq. (6a) achieves convergence, the values
of \( \alpha_k \) in Eq. (5b) and \( \beta_k \) in Eq. (6b), respectively, can
be regarded as weights of the tasks and the centralized regu-
larization. It is noteworthy that both \( \alpha_k \) and \( \beta_k \) are automati-
cally obtained without tuning parameters, i.e., parameter-
free. Moreover, if the \( t \)-task is important, then the predic-
tion error of both the loss function and the centralized regu-
larization are small. This indicates that our parameter-free
method is meaningful. Secondly, \( \bar{w} \) is the mean vector of \( w_t 
( t = 1, \ldots, k), \) while \( \alpha_t \beta_t \) is the weight to reduce the variance
of \( w_t \) in the term \( \alpha_t \beta_t \| w_t - \bar{w} \|_2^2 \) in Eq. (6b), i.e., making
all the tasks similar. Specifically, \( \alpha_t \beta_t \) is used to measure
the diversity and the flexibility of \( X_t. \) If \( X_t \) is more similar
to other tasks, the value of \( \alpha_t \beta_t \) should be bigger to push
\( w_t \) closer to \( \bar{w}. \) In this case, \( X_t \) has less flexibility (i.e., sex
specific patterns) and more stability (i.e., sex common patterns).
Moreover, the parameter-free optimization automatical-
ly balances contributions of sex specific patterns and sex
common patterns to the age prediction.

Convergence Analysis

The convergence of Algorithm 1 and Eq. (6a) is provided as
following. Particularly, the convergence of Eq. (6a) has been
proved in (Zhou, Chen, and Ye 2011). Algorithm 1 is a spe-
cial case of the Iteratively Re-weighted Least Square (IRLS)
framework (Daubechies et al. 2010; Zhu et al. 2017a), and
its convergence and effectiveness have been theoretically
verified. To do this, we have following lemma (Hu et al.
2017; Zhu et al. 2017b).

Lemma 1. For any positive real numbers \( u \) and \( v, \) following
inequality always holds:

\[
\sqrt{u} - \frac{u}{2\sqrt{v}} \leq \sqrt{v} - \frac{v}{2\sqrt{u}}. \tag{8}
\]

Theorem 1. The objective function value in Eq. (4) monoto-
ically decreases until Algorithm 1 converges.

Proof. We denote \( \hat{w}_t, \hat{w}, \) and \( \hat{\alpha}_t \) as the updated \( w_t, \bar{w}, \) and \( \alpha_t \)
in each iteration, and then present the convergence analysis
of Algorithm 1 via following three steps.
• Obtain $\hat{w}_t$ (t = 1, ..., k) while fixing $\hat{w}$, and $\alpha_t$.

We change Eq. (4) with respect to $w_t$ (t = 1, ..., k) to:

$$\hat{w}_t = \min \left\{ \sqrt{\|y_t - X_t w_t\|^2 + \|w_t - \hat{w}\|^2} \right\}
+ \gamma \|w_1, ..., w_t, ..., w_k\|_1$$

(9)

According to Eq. (5b) and Eq. (15), we have

$$\sum_{i=1}^{k} \left\{ \|y_i - X_i w_i\|^2 + \|w_i - \hat{w}\|^2 \right\} + \gamma \|\hat{w}\|_1$$

(10)

and

$$\sum_{i=1}^{k} \left\{ \|y_i - X_i w_i\|^2 + \|w_i - \hat{w}\|^2 \right\} + \gamma \|\hat{w}\|_1$$

(11)

By combining Eq. (10) with Eq. (11), we obtain

$$\|y_t - (X_t)_{:,i}(\hat{w}_t)\|^2 + \|\hat{w}_t\|_2,1 + \gamma (\hat{w}_t)_{:,i} \leq \|y_t - (X_t)_{:,i}(\hat{w}_t)\|^2 + \|\hat{w}_t\|_2,1 + \gamma (\hat{w}_t)_{:,i}$$

(12)

After summing all the $i$, we obtain

$$\|y_t - X_t \hat{w}_t\|^2 + \|\hat{w}_t\|_2,1 + \gamma \|\hat{w}_t\|_1$$

(13)

After summing all the tasks, we have

$$\sum_{t=1}^{k} \sqrt{\|y_t - X_t \hat{w}_t\|^2 + \|\hat{w}_t - \hat{w}\|^2} + \gamma \|\hat{w}\|_1$$

(14)

• Obtain $\hat{\hat{w}}$ while fixing $\hat{\hat{w}}$ and $\hat{\hat{w}}_t$ (t = 1, ..., k), and $\alpha_t$.

We change Eq. (4) with respect to $\hat{w}$ to:

$$\hat{\hat{w}} = \min \left\{ \sqrt{\sum_{i=1}^{k} \|y_i - X_i \hat{w}_i\|^2 + \|\hat{w}_i - \hat{w}\|^2} \right\}
+ \gamma \|\hat{w}\|_1$$

(15)

According to Lemma 1, we have

$$\sum_{i=1}^{k} \left\{ \|y_i - X_i \hat{w}_i\|^2 + \|\hat{w}_i - \hat{w}\|^2 \right\} + \gamma \|\hat{w}\|_1$$

(16)

and

$$\sum_{i=1}^{k} \left\{ \|y_i - X_i \hat{w}_i\|^2 + \|\hat{w}_i - \hat{w}\|^2 \right\} + \gamma \|\hat{w}\|_1$$

(17)

By combining Eq. (16) with Eq. (17), we obtain

$$\sum_{t=1}^{k} \sqrt{\|y_t - X_t \hat{w}_t\|^2 + \|\hat{w}_t - \hat{w}\|^2} + \gamma \|\hat{w}\|_1$$

(18)

• Obtain $\hat{\hat{w}}$ while fixing $\hat{\hat{w}}$ and $\hat{\hat{w}}_t$ (t = 1, ..., k).

According to Eq. (5b), $\alpha_t$ has a closed form solution, and thus Eq. (19) will be held.

Finally, the iterative optimization in Algorithm 1 will monotonically decrease the objective function value of Eq. (4) in each iteration until Algorithm 1 converges to a local optimization solution of Eq. (4).

Results

Experimental Settings

To evaluate our method, we compared it with following methods based on data from distinct groups, e.g., males and females, in a regression prediction setting.

Firstly, we conducted least square linear regression (Regression for short) (Friedman, Hastie, and Tibshirani 2001)
and Lasso (Tibshirani 1996) to build group specific prediction models upon the data points from each group separately.

Secondly, we built a single prediction model on pooled data points from all groups, regardless their group differences using either least square linear regression (ConRegression for short) or Lasso (ConLasso for short). And then, we estimated the performance of the prediction model for each group separately.

Thirdly, we used the group information as an extra feature to build a single prediction model using Lasso, referred to as MixLasso for short. We also estimated the performance of the prediction model for each group separately.

Lastly, by regarding the prediction for each group as a different task, we carried out multi-task learning with the standard multi-task learning method (MKL for short) (Zhu et al. 2016a; Argyriou, Evgeniou, and Pontil 2007; Zhu, Suk, and Shen 2014). Different from our method, the MKL method does not consider the weight of different tasks or the centralized regularization. All the methods were evaluated using 10-fold cross-validation. We repeated the whole process 20 times to avoid possible bias during data partitioning for cross-validation. The final results were average of all 20 experiments. For the model selection, the parameters of the regression method and the Lasso were tuned based on cross-validation, and we carried out a grid searching on the parameter $\lambda \in \{10^{-3}, ..., 10^3\}$ for MKL and our method.

In all experiments, the prediction performance was measured using Correlation Coefficient (CC) between the predicted and real values.

**Data**

**Synthetic data** We generated four synthetic datasets by setting different values for the number of groups ($k$), the number of features ($d$), and the number of samples ($n$). Specifically, each element of $X_t$ was sampled independent and identically distributed (i.i.d) from Gaussian distribution $N(0, 1)$ and then each feature was normalized to have a unit scale. Each element of the true $w_t$ was sampled i.i.d from the uniform distribution in the interval $[-5, 5]$. We randomly set zeros to 20% rows of $W$ and randomly replaced 60% elements of the remaining nonzero elements with zeros. Finally, noise $\delta_t$ sampled i.i.d from Gaussian distribution $N(0, 10)$ was added to the features. The response was computed as $y_t = X_t w_t + \delta_t$.

**PNC** The Philadelphia Neurodevelopmental Cohort (PNC) is a collaboration between the Center for Applied Genomics at Childrens Hospital of Philadelphia (CHOP) and the Brain Behavior Laboratory at the University of Pennsylvania (Penn) (Satterthwaite et al. 2014). We followed (Li, Satterthwaite, and Fan 2017) to conduct data preprocessing. All data in this study were acquired on the same scanner (Siemens Tim Trio 3 Tesla, Erlangen, Germany; 32-channel head coil) using the same imaging sequences. One T1 scan was acquired prior to the rsfMRI scan with 124 time-points for each subject and the T1 images were processed using Freesurfer. Each rsfMRI scan was first registered to its corresponding T1 image, and then was projected to the fsaverage surface space via Freesurfer after preprocessed using an optimized confound regression procedure (Li, Satterthwaite, and Fan 2017). Finally, we obtained preprocessed rsfMRI scans of 1401 subjects aged 8-22 years (651 males). We examined sex differences in 1540 edgewise RSFC measures within a brain network with 56 nodes described in (Li, Satterthwaite, and Fan 2017).

**Table 1:** CC results of Data 1 ($k=30$, $n=1000$, $d=400$) and Data 2 ($k=50$, $n=1000$, $d=2000$).

<table>
<thead>
<tr>
<th>Methods</th>
<th>Data 1</th>
<th>Data 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>ConRegression</td>
<td>0.735 ± 0.025</td>
<td>0.676 ± 0.022</td>
</tr>
<tr>
<td>ConLasso</td>
<td>0.745 ± 0.027</td>
<td>0.698 ± 0.025</td>
</tr>
<tr>
<td>MixLasso</td>
<td>0.749 ± 0.031</td>
<td>0.704 ± 0.023</td>
</tr>
<tr>
<td>MKL</td>
<td>0.766 ± 0.032</td>
<td>0.711 ± 0.015</td>
</tr>
<tr>
<td>Proposed</td>
<td>0.799 ± 0.012</td>
<td>0.763 ± 0.015</td>
</tr>
</tbody>
</table>

**Table 2:** CC results of Data 3 ($k=2$, $n=1000$, $d=400$).

<table>
<thead>
<tr>
<th>Methods</th>
<th>Task 1</th>
<th>Task 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regression</td>
<td>0.877 ± 0.173</td>
<td>0.851 ± 0.176</td>
</tr>
<tr>
<td>Lasso</td>
<td>0.889 ± 0.182</td>
<td>0.865 ± 0.195</td>
</tr>
<tr>
<td>ConRegression</td>
<td>0.878 ± 0.152</td>
<td>0.862 ± 0.232</td>
</tr>
<tr>
<td>ConLasso</td>
<td>0.890 ± 0.123</td>
<td>0.872 ± 0.214</td>
</tr>
<tr>
<td>MixLasso</td>
<td>0.909 ± 0.203</td>
<td>0.885 ± 0.167</td>
</tr>
<tr>
<td>MKL</td>
<td>0.923 ± 0.111</td>
<td>0.884 ± 0.202</td>
</tr>
<tr>
<td>Proposed</td>
<td>0.945 ± 0.112</td>
<td>0.921 ± 0.208</td>
</tr>
</tbody>
</table>

**Table 3:** CC results of Data 4 ($k=2$, $n=1000$, $d=2000$).

<table>
<thead>
<tr>
<th>Methods</th>
<th>Task 1</th>
<th>Task 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regression</td>
<td>0.758 ± 0.054</td>
<td>0.801 ± 0.027</td>
</tr>
<tr>
<td>Lasso</td>
<td>0.767 ± 0.015</td>
<td>0.804 ± 0.031</td>
</tr>
<tr>
<td>ConRegression</td>
<td>0.785 ± 0.084</td>
<td>0.801 ± 0.047</td>
</tr>
<tr>
<td>ConLasso</td>
<td>0.788 ± 0.044</td>
<td>0.804 ± 0.028</td>
</tr>
<tr>
<td>MixLasso</td>
<td>0.796 ± 0.036</td>
<td>0.811 ± 0.035</td>
</tr>
<tr>
<td>MKL</td>
<td>0.805 ± 0.045</td>
<td>0.812 ± 0.045</td>
</tr>
<tr>
<td>Proposed</td>
<td>0.837 ± 0.024</td>
<td>0.842 ± 0.018</td>
</tr>
</tbody>
</table>

**Table 4:** CC results of PNC data.

<table>
<thead>
<tr>
<th>Methods</th>
<th>Males</th>
<th>Females</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regression</td>
<td>0.562 ± 0.017</td>
<td>0.397 ± 0.022</td>
</tr>
<tr>
<td>Lasso</td>
<td>0.566 ± 0.014</td>
<td>0.400 ± 0.025</td>
</tr>
<tr>
<td>ConRegression</td>
<td>0.566 ± 0.014</td>
<td>0.421 ± 0.024</td>
</tr>
<tr>
<td>ConLasso</td>
<td>0.567 ± 0.013</td>
<td>0.438 ± 0.021</td>
</tr>
<tr>
<td>MixLasso</td>
<td>0.571 ± 0.013</td>
<td>0.414 ± 0.017</td>
</tr>
<tr>
<td>MKL</td>
<td>0.581 ± 0.016</td>
<td>0.452 ± 0.028</td>
</tr>
<tr>
<td>Proposed</td>
<td>0.599 ± 0.012</td>
<td>0.495 ± 0.027</td>
</tr>
</tbody>
</table>

**Result analysis: Synthetic datasets**

We summarize the CC results of all the methods on four different datasets in Tables 1-3 to illustrate the effectiveness of our proposed method for datasets with different numbers of groups, different number of features, as well as different numbers of samples.
From Tables 1 and 2, we observe that our proposed method outperformed all alternative methods under comparison on different kinds of datasets such as \( d \leq n \) in Table 1 and \( d \geq n \) in Table 2. For example, our method improved on average by 11.3% and 7.9, respectively, compared with the worst comparison method (i.e., ConRegression) and the best comparison methods (i.e., MKL) on two synthetic datasets. These results indicate that our assumption (i.e., making use of sex specific and common patterns) is reasonable and our proposed method is robust.

Table 3 demonstrates that our method also outperformed all alternative methods under comparison on 2 two-task datasets with the same number of groups as the PNC data. Firstly, feature selection methods (such as Lasso, ConLass, MixLasso, MKL, and our proposed method) outperformed regression methods using all the features (such as Regression and Con-Regression), indicating that the feature selection methods were robust to noisy features in the synthetic datasets. Secondly, different groups had different regression performance, highlighting differences among different groups. Thirdly, concatenation methods (i.e., ConRegression and ConLasso) did not always outperform the corresponding single-task regression methods since heterogeneous data may degrade the prediction performance. These observations indicate that the prediction performance could be improved only if all prediction tasks are modeled effectively, as demonstrated by the results of MKL and our method in Tables 2-3.

**Result analysis: PNC data**

**Sex differences detected by the single prediction model**

We summarize the prediction results of Regression and Lasso in Table 4, highlighting the developmental sex differences in RSFC measures. Moreover, the age prediction for males outperformed the age prediction for females in terms of the values of coefficient correlation.

In our experiments, we ran our algorithm 200 times (via repeating 10-fold cross validation 20 times) and in each run we kept the features with nonzero coefficients for Lasso. We calculated the frequency of each feature appearing in all these 200 experiments and identify top selected features, i.e., top 50, for each group. We visualize the common patterns among two groups and sex specific RSFC patterns, comprising the selected RSFC features in Figure 1. As shown in Figure 1, Default, Visual, and Frontoparietal networks were sex common networks, while the prediction of age for females selected Visual networks with a higher frequency and the prediction of age for males selected Frontoparietal more frequently. Moreover, Limbic was the least frequently selected network for both the males and females. All the above results are largely consistent with findings in existing studies (Yeo et al. 2011; Satterthwaite et al. 2013).

**Sex differences detected by the prediction models in the multi-task learning framework**

According to Table 4, our method achieved the best prediction performance, followed by MKL, MixLasso, ConLasso, ConRegression, Lasso, and Regression. For example, our method improved on average by 12.35% and 5.82%, respectively, over Lasso and MKL. We also carried out non-parametric paired-sample tests (at 95% significance level) between the results of our method and the results of each alternative method under comparison, and the results indicated that our proposed method outperformed other methods with statistical significance. These results indicate that multi-task learning (such as MKL and our method) may make better use of sex specific and common patterns for predicting age. Moreover, our method outperformed MKL since our method takes into consideration the importance of the groups and the balance of sex specific and common patterns.

Our method in Eq. (4) simultaneously generated two prediction models (i.e., \( w_1 \) and \( w_2 \), one for each group). Moreover, these two coefficient vectors were sparse. Accordingly, we calculated the frequency of the selected features, and then visualize the corresponding brain networks in Figure 2. From Figure 2, we observe that our method identified RSFC patterns similar to the results in single group. For example, our method also selected RSFC measures among Default, Visual, and Frontoparietal networks as the most important features for the age prediction. In contrast to the previous results, the RSFC measures identified by our method were selected with a higher frequency, indicating that our method had higher reliability than the single group method.

In summary, our method achieved the best prediction performance as well as identified RSFC patterns underlying the developmental sex difference with improved reliability.

**Discussion and conclusions**

**Parameter sensitivity**

We have shown the variations of CC of our method at different settings of the parameter \( \gamma \) in Figure 3. We observe that the best performance of our method improved on average by 10 compared with the worst case at different datasets, and our method achieved its best results when the sparsity ratio was about 30% \( \sim \) 60%. These observations indicate that our method is sensitive to the parameter setting. In our method, we use a square root loss function and an \( \ell_{2,1} \)-norm regularization to reduce two more parameters to make our algorithm fast. Our method circumvents the parameter tuning problem.

**Convergence analysis**

In Section Optimization, we have theoretically proved the convergence of the proposed algorithm for solving Eq. (4). Figure 4 experimentally demonstrates the convergence of the proposed Algorithm 1, showing the objective function values of Eq. (4) on the iteration steps until Algorithm 1 converges. These experimental results indicate that the proposed Algorithm 1 can effectively tackle Eq. (4) with a fast convergence within tens of iteration steps.

In conclusion, we proposed a novel parameter-free centralized multi-task learning method to automatically learn the importance of different tasks and the balance of the distinct and common information associated with the tasks. The experimental results based on both synthetic and real rsfMRI data have demonstrated that our method outperformed the alternative methods under comparison in term of the prediction performance. Furthermore, our method could also...
identify informative RSFC patterns that are predictive for the brain development.

References


Figure 4: Parameter sensitivity on $\gamma$ of our method at different datasets. Note that PNC (t1) indicates the results of PNC task 1.